



**Figure 5.6** The general case for alpha–beta pruning. If  $m$  or  $m'$  is better than  $n$  for Player, we will never get to  $n$  in play.

```
function ALPHA-BETA-SEARCH(game, state) returns an action
  player  $\leftarrow$  game.TO-MOVE(state)
  value, move  $\leftarrow$  MAX-VALUE(game, state,  $-\infty$ ,  $+\infty$ )
  return move
```

```
function MAX-VALUE(game, state,  $\alpha$ ,  $\beta$ ) returns a (utility, move) pair
  if game.IS-TERMINAL(state) then return game.UTILITY(state, player), null
  v, move  $\leftarrow$   $-\infty$ , null
  for each a in game.ACTIONS(state) do
    v2, a2  $\leftarrow$  MIN-VALUE(game, game.RESULT(state, a),  $\alpha$ ,  $\beta$ )
    if v2 > v then
      v, move  $\leftarrow$  v2, a
       $\alpha \leftarrow$  MAX( $\alpha$ , v)
    if v  $\geq$   $\beta$  then return v, move
  return v, move
```

```
function MIN-VALUE(game, state,  $\alpha$ ,  $\beta$ ) returns a (utility, move) pair
  if game.IS-TERMINAL(state) then return game.UTILITY(state, player), null
  v, move  $\leftarrow$   $+\infty$ , null
  for each a in game.ACTIONS(state) do
    v2, a2  $\leftarrow$  MAX-VALUE(game, game.RESULT(state, a),  $\alpha$ ,  $\beta$ )
    if v2 < v then
      v, move  $\leftarrow$  v2, a
       $\beta \leftarrow$  MIN( $\beta$ , v)
    if v  $\leq$   $\alpha$  then return v, move
  return v, move
```

**Figure 5.7** The alpha–beta search algorithm. Notice that these functions are the same as the MINIMAX-SEARCH functions in Figure 5.3, except that we maintain bounds in the variables  $\alpha$  and  $\beta$ , and use them to cut off search when a value is outside the bounds.